# Sample size estimation 

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## Why do we need a sample size estimation

- To make sure the study have adequate power to show a difference to be significant
- Un-sufficient sample size not able to show an important difference
- Un-necessarily large sample size will waste resources
- Statistically significant difference may not have clinical importance


## Factors affecting sample size estimation

- Magnitude of the difference (between the two comparison groups)
- Standard deviation of the outcome measures
- Pre-specified significant level of the statistical test (default value=0.05) and
- Pre-specified power of the statistical test (default value=80\%)


## Example 1: sample size estimation for comparison on two mean values

- To compare average height between boys and girls at 12-14 year's of age
- Mean height of boys $=147 \mathrm{~cm}$
- Mean height of girls=152cm
- Standard Deviation (SD) $=8 \mathrm{~cm}$
- How many samples we need to show 5 cm difference to be significant


## Example 1 (continue): sample size estimation for comparison on two mean values

- We need 41 in each group (82 in total)


## Sample size requirement in relation to magnitude of difference and SD

| mean1 <br> $(\mathrm{cm})$ | mean2 <br> $(\mathrm{cm})$ | Difference <br> of mean <br> values $(\mathrm{cm})$ | SD <br> $(\mathrm{cm})$ | Sample size <br> required in <br> each group <br> $(\mathrm{n} 1)$ |
| :---: | :---: | :---: | :---: | :---: |
| 145 | 152 | 7 | 8 | 21 |
| 147 | 152 | 5 | 8 | 41 |
| 149 | 152 | 3 | 8 | 112 |

- The smaller the difference, the larger the sample size
- The larger the SD, the larger the sample size required


## Example 2: 6MWT

- A research group want to investigate whether hospital inpatients after knee replacement would have better outcome, measured by six minutes walking test (6MWT), compared to patients going home after knee replacement
- What information we need for a sample size calculation?


## Example 2 (continue): 6MWT

- Mean distance 6MWT = 400 m (inpatient group)
- Mean distance $6 \mathrm{MWT}=330 \mathrm{~m}$ (home group)
- $\mathrm{SD}=100 \mathrm{~m}$
- Assume (by default): alpha=0.05, power=80\%
- To show the difference between 400 m and 330 m to be statistically significant
- How many sample do we need?


## Online calculator for sample size

- https://www.stat.ubc.ca/~rollin/stats/ssize/n2.html


## Inference for Means: Comparing Two Independent Samples

(To use this page, your browser must recognize JavaScript.)
Choose which calculation you desire, enter the relevant population values for mu1 (mean of population 1), mu2 (mean c for each sample). You may also modify $\alpha$ (type I error rate) and the power, if relevant. After making your entries, hit the

- Calculate Sample Size (for specified Power)
- Calculate Power (for specified Sample Size)

Enter a value for mur 400
Enter a value for mue: 330
Enter a value for sigma: 100

- 1 Sided Test
- 2 Sided Test

Enter a value for $\alpha$ (default is . 05 ):
Enter a value for desired power (default is .80):

| .05 |
| :--- |
| .80 |
| 33 |

The sample size (for each sample separately) is:33

## Calculate

- need 33 in each group (66 in total)


## Example 3: sample size estimation for a RCT study

- The research question is: whether a new drug to be more efficient as a treatment of hypertension compared to the current standard drug. The sitting diastolic blood pressure (SDBP) will be measured at baseline and then 3 month later. Change of SDBP will be used as primary outcome measure


## Example 3 (continuous) : RCT study

- mean change of SDBP in new treatment group $=18 \mathrm{~mm} \mathrm{Hg}$
- Mean change in the control group=14 mm Hg
- $\mathrm{SD}=9 \mathrm{~mm} \mathrm{Hg}$
- Alpha= 0.05 , power= $80 \%$
- 1:1 ratio between two randomisation groups


## Using online calculator:

## Inference for Means: Comparing Two Independent Samples

(To use this page, your browser must recognize JavaScript.)
Choose which calculation you desire, enter the relevant population values for mu1 (mean of population 1 ), mu2 ( for each sample). You may also modify $\alpha$ (type I error rate) and the power, if relevant. After making your entries,

- Calculate Sample Size (for specified Power)
- Calculate Power (for specified Sample Size)

Enter a value for mus: 18
Enter a value for muR: 14
Enter a value for sigma: 9

- 1 Sided Test
- 2 Sided Test

Enter a value for $\alpha$ (default is . 05 ):
Enter a value for desired power (default is .80): $\square$
The sample size (for each sample separately) is: 80

Calculate

- The study will need to recruit 80 sample in each randomisation group (160 in total)


## Statistical significant versus clinical important

- The difference between two (treatment) groups should have clinical meaning
- Clinical benefit should be based on findings from the literature or historical knowledge
- Minimal clinically important difference (MCID) https://en.wikipedia.org/wiki/Minimal clinically important difference
- e.g. 0.5 point difference in QOL to be clinically meaningful
- e.g. 70 meter difference in 6MWT


## Example 4: sample size calculation for comparing two proportions

- To compare the prevalence of wheeze in the last 12 month between 8-10 year's old boys and girls
- Boys tends to have higher prevalence of recent wheeze in this age range than girls
- To show a $24 \%$ of wheeze in boys to be significantly different to a $9 \%$ of wheeze in girls, how many samples (per group) do we need?


## Example 4 (continue): comparison of two proportions

- $\mathrm{P}_{1}$ (in boys)=24\%
- $\quad \mathrm{P}_{2}$ (in girls) $=9 \%$
- Assume significant level=0.05, power=80\%
- How many sample do we need?
- Answer: need 93 in each group


## Example 5: 'translate' original research question:

- To investigate that the sub-therapeutic levels occurs with higher frequency where there is a suspicion of LOR by biochemical or clinical parameters (and are more common than in those patients on maintenance therapy without suspicion of LOR)
- To do sample size estimation, we need to translate this research question into a hypothesis testing question


## Example5 (continue): comparing two proportions

- To compare the occurrence of sub-therapeutic levels to be higher in suspicion of LOR patients compared to no-suspicion of LOR patients
- $\mathrm{p}_{1}=$ proportion of 'sub-level' = $15 \%$ in group 1 $\mathrm{p}_{2}=$ proportion of 'sub-level' $=7 \%$ in group 2
- Assume suspicion of LOR and no-suspicion of LOR to be 50:50 in patients


## Online calculator for sample size calculation

- https://www.stat.ubc.ca/~rollin/stats/ssize/b2.htmil


## Inference for Proportions: Comparing Two Independent Samples

(To use this page, your browser must recognize JavaScript.)
Choose which calculation you desire, enter the relevant population values (as decimal fractions) for p 1 (proportion in F sample). You may also modify $\alpha$ (type I error rate) and the power, if relevant. After making your entries, hit the calcula

- Calculate Sample Size (for specified Power)
- Calculate Power (for specified Sample Size)

Enter a value for $\mathbf{p} 10.15$
Enter a value for $\mathbf{p}: 0.07$

- 1 Sided Test
- 2 Sided Test

| Enter a value for $\boldsymbol{\alpha}$ (default is $\mathbf{. 0 5}$ ): | .05 |
| :--- | :--- |
| Enter a value for desired power (default is $\mathbf{8 0}$ ): | .80 |
| The sample size (for each sample separately) is: | 239 |

## Calculate

- need 239 in each group (478 in total)


## Where to find information on mean difference and SD?

- From literature, other studies with the same measurements
- Studies with the same outcome measure but with slightly different study population
- Conducting a pilot study


## What if SD not known

- 3 SD on either side of the mean value will cover $99.7 \%$ of the sample
- SD ~ (max - min) / 6 = range / 6


## Two group comparison with un-equal sample per group

- Look at example 5 again (suspicion of LOR example)
- If with 1:1 ratio, we need 239 in each group (478 in total)
- What if there are $75 \%$ who would have suspicion of LOR (25\% non-suspicion)
- Sample size calculation assuming 3:1 ratio


## Sample size calculation for 3:1 ratio

## http://powerandsamplesize.com/Calculators/Compare-2- <br> Proportions/2-Sample-Equality



Power, $1-\beta$

```
Type I error rate, ox
```



```
Group 'A' Proportion, pA
Group 'B' Proportion, pB
Sampling Ratio, }\kappa=\mp@subsup{n}{A}{}/\mp@subsup{n}{B}{
```

Calculate

- We need 132 in non-LOR group, and 3x132=396 in LOR group, i.e. 528 in total for 3:1 ratio


## What if there are drop outs in follow up studies

- Conducting a sample size calculation (assume no drop out first)
- Inflate the sample size by the possible drop out rate (say 15\%)
- For a $15 \%$ drop out, multiply sample size by 1.15 approximate


## Online calculator for sample size calculation

- http://powerandsamplesize.com/Knowledge/
- http://powerandsamplesize.com/Calculators/
- https://www.stat.ubc.ca/~rollin/stats/ssize/n2.htm|


## Thank you

# Introduction to Statistical Analysis Basic concepts and hypothesis testing 

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## Outline

- Types of Data
- Descriptive Statistics
- Numerical summaries
- Graphical Summaries
- Hypothesis Testing
- Null and alternative hypothesis


## TYPES OF DATA

## Continuous data

## Data that can take

 on any value (within a range)
## Also referred to as Scale Data



## Binary data

Categorical Data with $\mathbf{2}$ categories



## Nominal data

Categorical Data with more than 2
 categories


## Ordinal data

Categorical Data with ordered categories


## DESCRIPTIVE STATISTICS

## Continuous data summaries

## Measures of Central Tendency

- Mean (Average)
- Median (50 ${ }^{\text {th }}$ Percentile)


## Measures of Spread

- Standard Deviation
- Lower and upper quartiles ( $25^{\text {th }}$ and $75^{\text {th }}$ Percentile respectively)
- Interquartile Range ( $75^{\text {th }}$ Percentile $-25^{\text {th }}$ Percentile)
- Range (Maximum - Minimum)


## Standard Deviation (SD)

- Useful for normally distributed data (more on this later)
- Larger standard deviation indicates more variability

| Gender | N | Mean Height | Standard Deviation |
| :---: | :---: | :---: | :---: |
| Females | 150 | 145 cm | 10 cm |
| Males | 150 | 150 cm | 5 cm |
| $\approx 68 \%$ of your data fall within 1 standard deviation <br> $\approx 95 \%$ of your data fall within 2 standard deviations |  |  |  |
|  |  |  |  |
| $\approx 99.7 \%$ of your data fall within 3 standard deviations |  |  |  |

## Histogram



## Histogram



4 people with a height between 149 and 150 cm's

5 people with height between 150 and 151 cm's

3 people with height between 151 and 152 cm's

## Histogram (Bin Size)



## Histogram (Y-axis)



$$
\begin{array}{llllll}
135 & 141 & 147 & 153 & 159 & 165
\end{array}
$$



## Histogn



## Histogram and SDs

| Gender | N | Mean Height | SD |
| :---: | :---: | :---: | :---: |
| Females | 150 | 145 cm | 10 cm |
| $68 \%$ of Betwee 55) | 135 | $1 \text { SD) }$ <br> and |  |

$\approx 95 \%$ of data (2 SD) ${ }^{5}$
(Between 125 and 165)
₹ 99.7\% of data (3 SD) (Between 115 and 175)

## Skewed Data



## Range

Students Heights


Students Heights

| 150 cm |  |
| :--- | :--- |
| 151 cm |  |
| 152 cm |  |
| 153 cm | Range | 35 cm

## Percentiles

Students Heights

$25^{\text {th }}$ Percentile Point where at least $25 \%$ of total data falls below
$75^{\text {th }}$ Percentile Point where at least 75\% of total data falls below

## Interquartile Range

Students Heights
150 cm

151 cm
152 cm
153 cm
154 cm
155 cm
156 cm
157 cm
180 cm

IQR represents of where the middle $50 \%$ of your data is
$\underline{I Q R}=156-152=4 \mathrm{~cm}$

Larger IQR suggests more spread/variability



## Continuous Data Summary

Measure of Measure of Spread Central Tendency<br>Mean<br>Median<br>(50 ${ }^{\text {th }}$ Percentile)<br>Standard Deviation<br>Lower Quartile<br>Upper Quartile<br>Interquartile Range

At minimum display either the Mean with Standard Deviation together, or Median (preferable when data is skewed) with percentiles

## Categorical Data

- Numerical Summaries
- N / counts
- Percentages / proportions
- Mode - Most frequent category
- Confidence Intervals
- Graphical summaries
- Bar Charts
- Clustered Bar Charts


## One Categorical Variable



## Two Categorical Variables

- Table Structure (2x2)

|  | Outcome |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Level 1 |  | Level 2 |  |
|  | n | \% | n | \% |
| Predictor 1 |  |  |  |  |
| Level 1 | a | Row \% | b | Row \% |
| Level 2 | c | Row \% | d | Row \% |
| Compare these Compare these |  |  |  |  |
| \% against each \% against each |  |  |  |  |

## $2 \times 2$ Tables



Males are more likely to be over 150 cm

Females are
more likely to be
less than 150 cm

## Clustered Bar Charts



## Other graphs?



## HYPOTHESIS TESTING

## Hypothesis testing

## Research question

Do knee surgery patients that undergo a newly created advanced (but expensive) rehabilitation protocol after surgery, experience an improved quality of life (QOL) compared with patients that undergo standard rehab protocol 3 months after surgery?

## Hy 0 thesis testing

Two group comparison with a continuous outcome measure.

What is the specific outcome measure?

Trying to prove a difference or equality in the outcome between the groups?

In which direction are you trying to prove difference/equality in the outcome measure between the groups?

What is the magnitude of difference or equality?

## Hymothest

Two group comparison with a continuous outcome measure.

What is the specific outcome measure?
QOL?? $\rightarrow$ Oxford Knee Score (0-48) (Lower score indicates worse knee arthritis)
Trying to prove a difference or equality in the outcome between the groups?
Difference
In which direction are you trying to prove difference/equality in the outcome measure between the groups?
Increase in OKS for the advanced group.
What is the magnitude of difference or equality?
Minimum clinically important difference for OKS $=5$ (Clement et al.)

## Hypothesis testing

Null hypothesis: The OKS is not higher in the advanced group by at least 5 units compared to the standard care group.

Alternative hypothesis: The OKS is higher by at least 5 units for the advanced group compared with the standard care group.

## Hypothesis testing

## Research question

Is there a difference in the number of circulating
tumour cells (CTC) between patients with stage 2 and stage 3 cancers?

## Hy 0 thesis testing

Two group comparison with a continuous outcome measure.

What is the specific outcome measure?
Circulating tumour cells (CTC)
Trying to prove a difference or equality in the outcome between the groups?
Difference
In which direction are you trying to prove difference/equality in the outcome measure between the groups?
Not specified in research question, though could expect to observe patients with stage 3 to have more CTCs than patients with stage 2 cancer.
What is the magnitude of difference or equality?
?? - Need to review literature to determine what is clinical difference in CTCs

## Hypothesis testing

Null hypothesis: There is no difference in the CTCs between stage 2 and 3 cancers. Alternative hypothesis: There is a difference in the CTCs between stage 2 and 3 cancers.

Null hypothesis: Patients with stage 3 cancers do not have more CTCs than patients with stage 2 cancers. Alternative hypothesis: Patients with stage 3 cancers have more CTCs than patients with stage 2 cancers.

## Hypothesis testing

## Research question

Do knee surgery patients that undergo a new rehabilitation program which is cheaper and requires less resources experience similar QOL outcomes 3 months after surgery compared with current standard care?

## Hy 0 thesis testing

Two group comparison with a continuous outcome measure.

What is the specific outcome measure?
Not specified - go with Oxford Knee score (OKS) again
Trying to prove a difference or equality in the outcome between the groups?
Equality
In which direction are you trying to prove difference/equality in the outcome measure between the groups?
Not specified, though could argue that only interested in outcome that is clinically worse.
What is the magnitude of difference or equality?
MCID OKS = 5 (Clement et al.)

## Hypothesis testing

Null hypothesis: OKS is at least 5 units lower in the new rehab program than compared with standard care.

Alternative hypothesis: OKS is no less than 5 units lower in the new rehab program compared with standard care.

## Hypothesis testing

Translate your research question into a set of null and alternative hypothesis.

The way the hypotheses are set up have an influence on sample size, study design, and statistical analysis (topics of future seminars).

These can be extended to more groups and different types of outcomes.

## References

Clement, N. D., et al. (2014). "The minimal clinically important difference in the Oxford knee score and Short Form 12 score after total knee arthroplasty." Knee Surg Sports
Traumatol Arthrosc 22(8): 1933-1939.

